



AUBURN UNIVERSITY

SAMUEL GINN  
COLLEGE OF ENGINEERING

# PROPOSED RE-CALIBRATION OF AASHTO LRFD SPECIFICATIONS

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# Calibration of Design Code

- **Bridges have to be designed with an adequate safety margin**
- **In LRFD Specifications safety is represented by load and resistance factors**
- **Code calibration is selection of load and resistance factors so that safety is at an acceptable level**

# Three Important Questions in Code Calibration

- **How to measure safety?**
- **What is acceptable safety level?**
- **How to select load and resistance factors so that safety is at acceptable level?**

# What is needed?

- **Statistical parameters of load**
- **Statistical parameters of resistance**
- **Reliability analysis procedure to calculate the Reliability Index**
- **Target Reliability Index**

# Statistical Parameters

- **Mean value**
- $\lambda = \text{Bias factor} = \text{mean/nominal}$
- $\sigma = \text{Standard deviation}$
- $V = \text{Coefficient of variation} = \sigma/\text{mean}$
- **Type of distribution function**

# Calibration of AASHTO LRFD 1994

- **Live load parameters based on Ontario truck survey in 1977**
- **Resistance parameters (concrete, reinforcing steel, prestressing strands, structural steel) based on test results in 1970's**
- **Reliability analysis procedure based on techniques from 1980's**

# What is new?

- **Over 200 million Weigh-in-Motion (WIM) records of trucks (national data base)**
- **New material test results (ordinary concrete, light-weight concrete, rebars, prestressing strands, structural steel)**
- **Simulation techniques (Monte Carlo)**
- **More efficient reliability analysis procedure (reliability index and design point)**

# What is the effect of new data?

- **Are current live loads different than Ontario data (1977)?**
- **Are new statistical parameters of resistance different than in 1970's?**
- **Are target reliability indices in AASHTO Specifications adequate?**
- **Are load and resistance factors in AASHTO Specifications adequate?**



# What is the difference?

- **A preliminary analysis of WIM data shows that the bias factor for live load is 5-10% larger than what was assumed in the original calibration, in particular for short spans**
- **A preliminary analysis of material strength test data shows that the load carrying capacity can be larger than previously assumed by 5-10%**

# Need for Re-Calibration

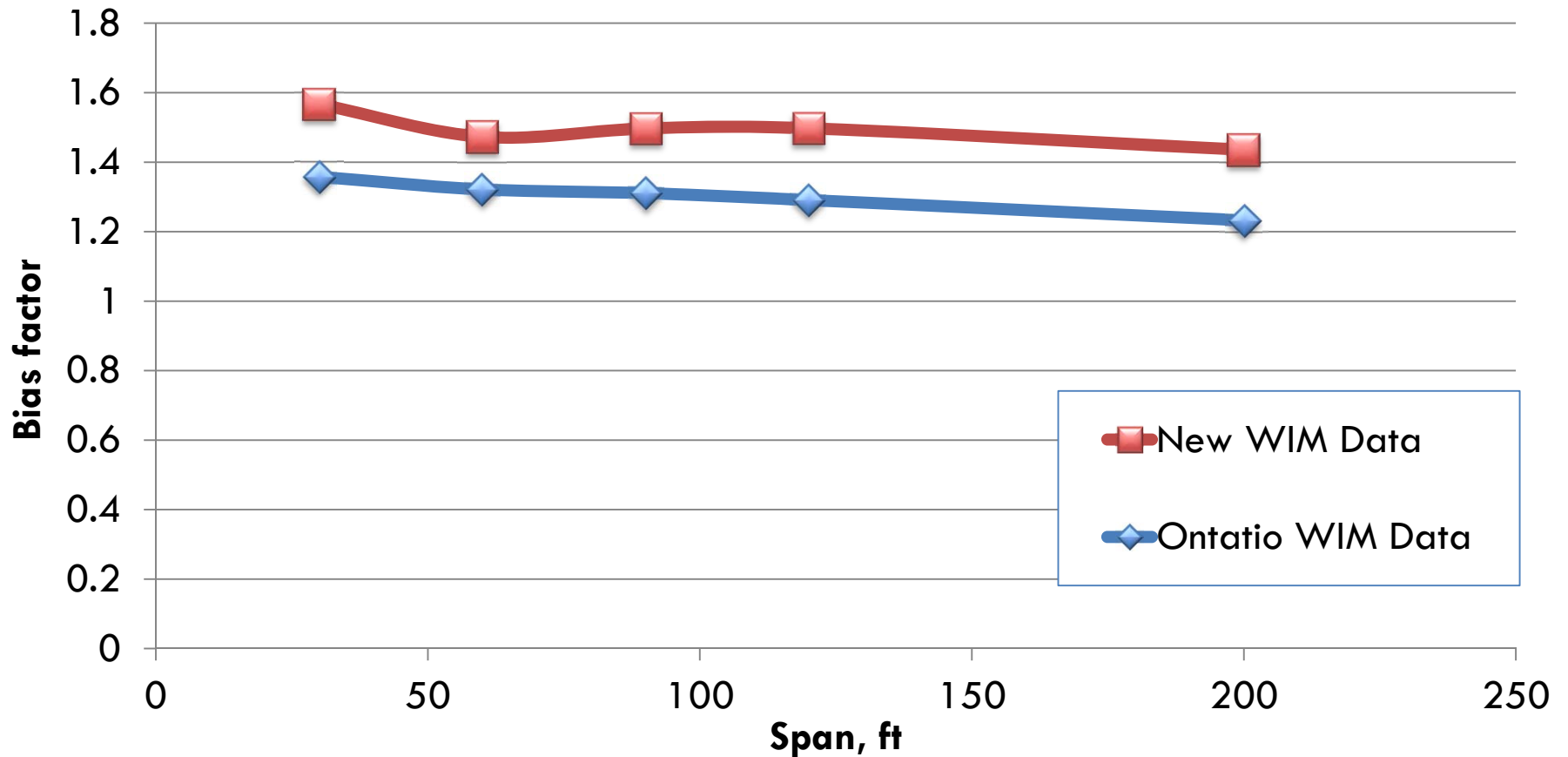
- **Revise the statistical parameters of load and resistance**
- **Select the target reliability index**
- **Calculate load and resistance factors as coordinates of the “design point”**
- **Compare with the current load and resistance factors and if needed, make recommendation for changes in AASHTO**

# Expected Results

- **Design point analysis can result in lower load and resistance factors**
- **Live load factor can be increased because of increase in live load**
- **Resistance factors can be increased because of increase in material strength, however, effect of quality of workmanship has to be assessed**

# New vs. Old Live Load - Moment

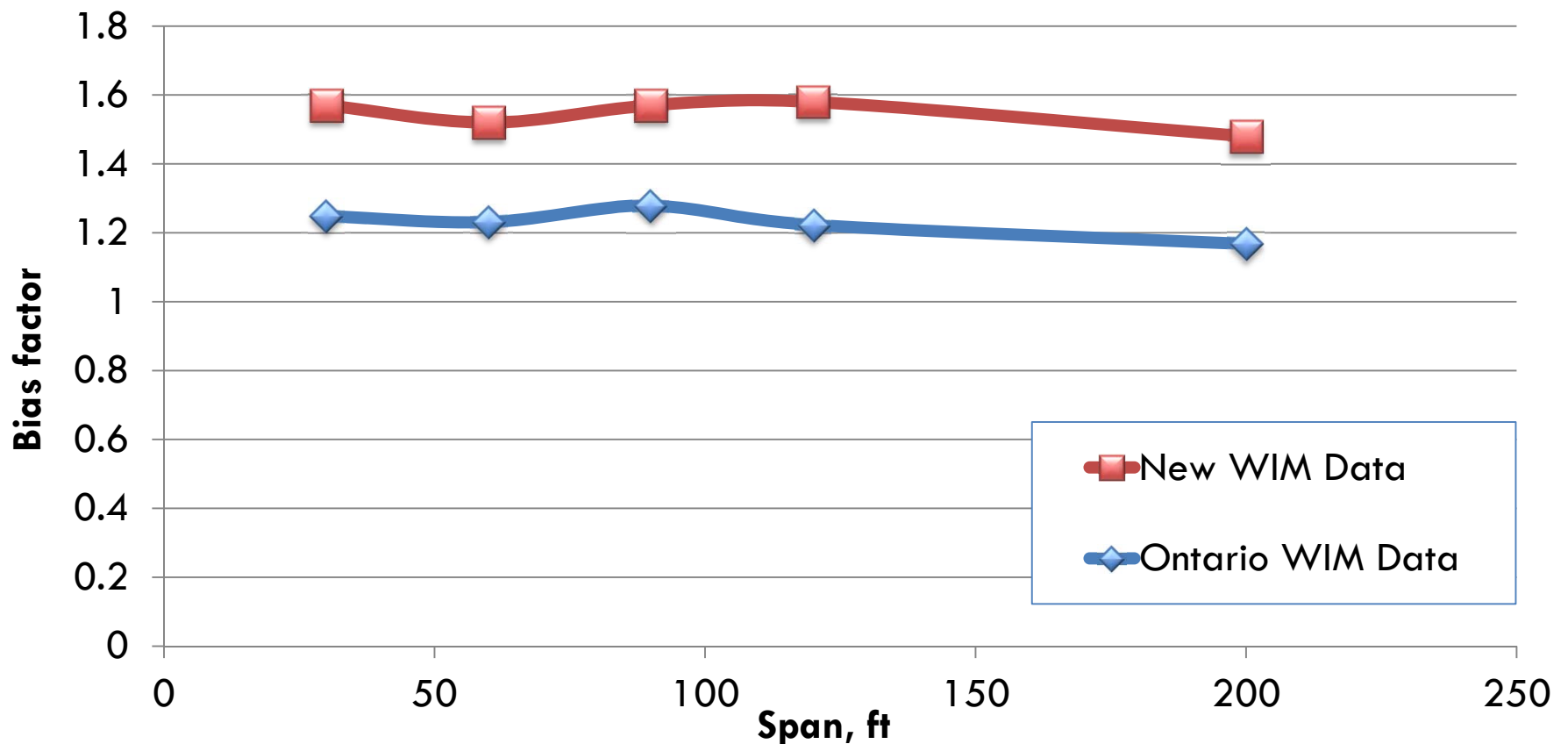
Mean Maximum 75 year Moments for Simple Spans Due to Multiple Trucks in One Lane (Divided by Corresponding HL-93 Moment) – ADTT=1000



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# New vs. Old Live Load - Shear

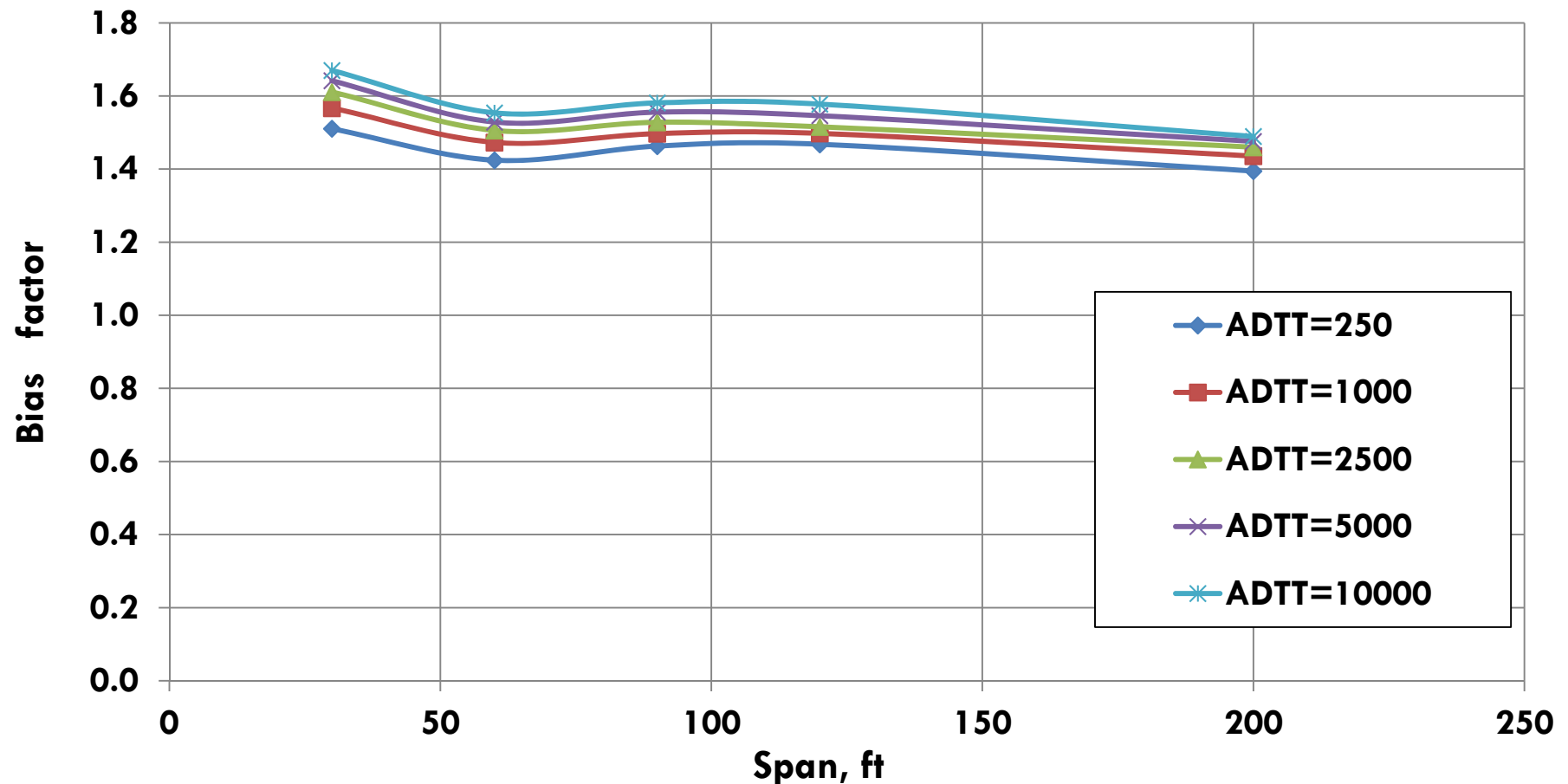
Mean Maximum 75 year Shear Force for Simple Spans Due to Multiple Trucks in One Lane (Divided by Corresponding HL-93 Moment) – ADTT=1000



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# New Live Load – Moment ratios

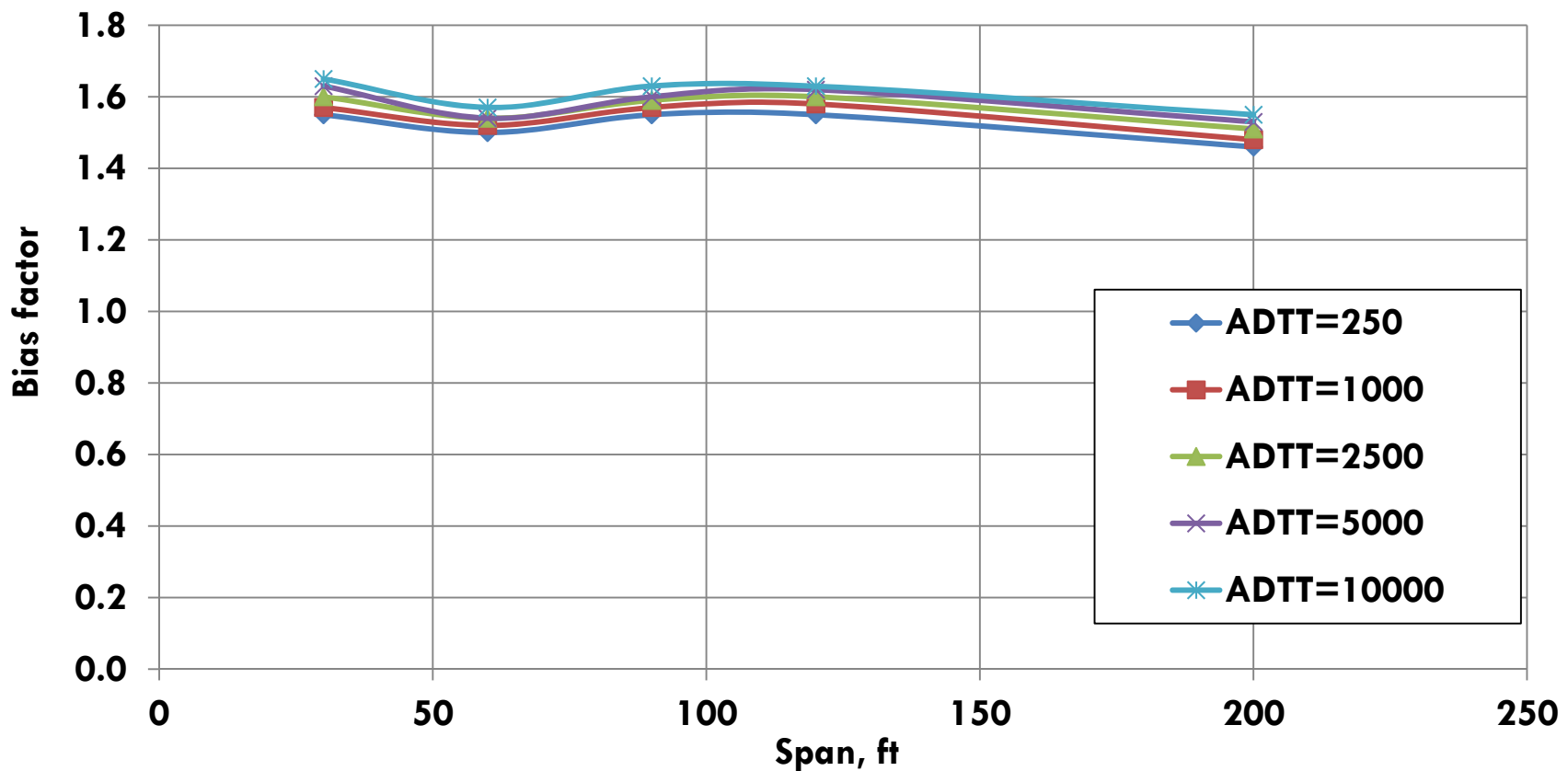
Mean Maximum 75 year Moment Ratio for Simple Spans Due to Multiple Trucks in One Lane (Divided by Corresponding HL-93 Moment) – ADTT=250...10,000



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# New Live Load – Shear ratios

Mean Maximum 75 year Moment Ratio for Simple Spans Due to Multiple Trucks in One Lane (Divided by Corresponding HL-93 Shear) – ADTT=250...10,000



# Parameters of Resistance

- **M = Material** : uncertainty in the strength of material, modulus of elasticity, cracking stresses, and chemical composition.
- **F = Fabrication** : uncertainty in the overall dimensions of the component which can affect the cross-section area, moment of inertia, and section modulus.
- **P = Analysis** : uncertainty resulting from approximate methods of analysis and idealized stress/strain distribution models.



# Resistance (load carrying capacity)

$$R = R_n M F P$$

where :

$R_n$  = nominal value of resistance

$M$  = material factor

$F$  = fabrication factor

$P$  = professional factor

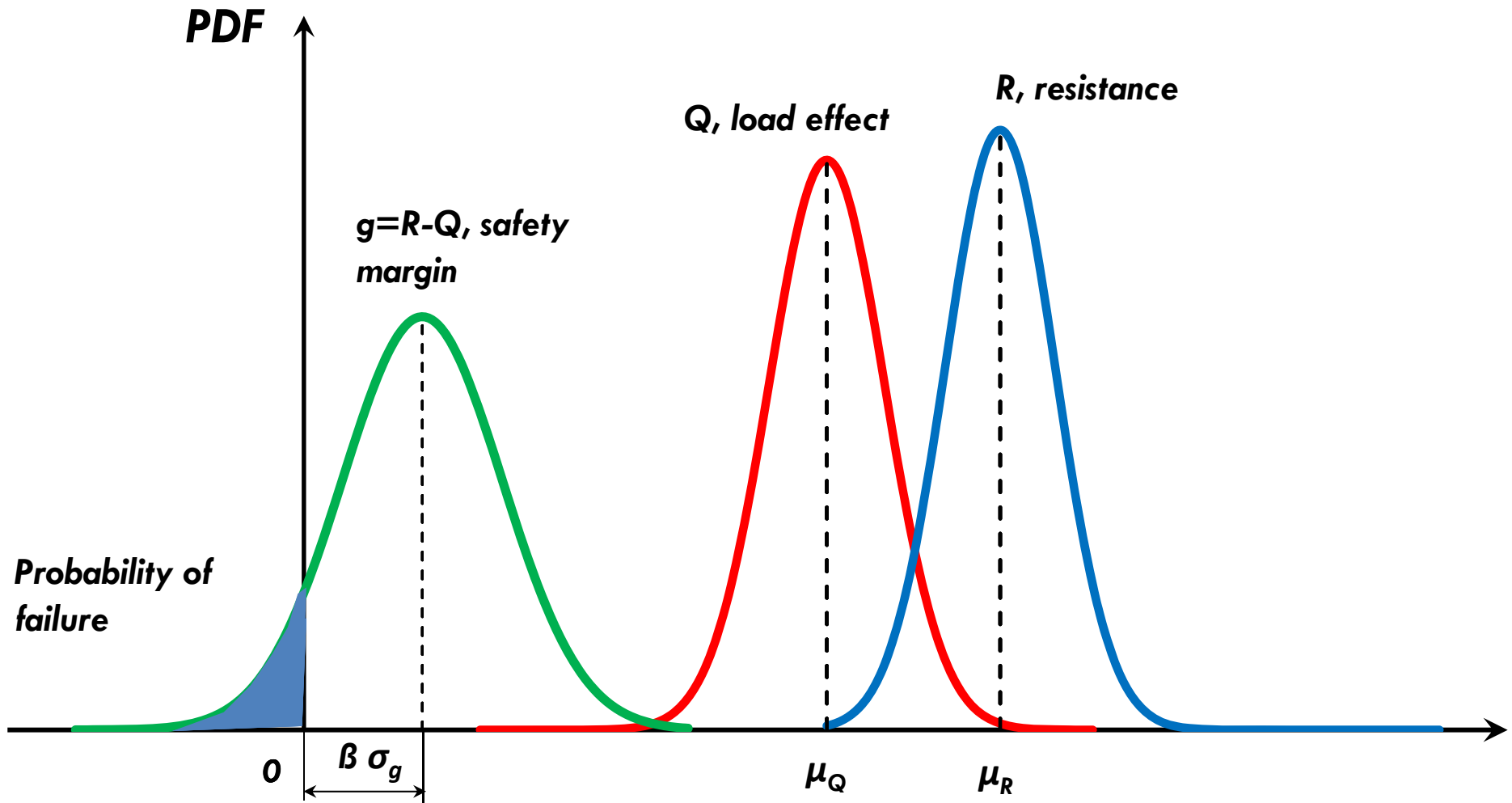
# What is affected?

- **Bias factor = ratio of mean-to-nominal**
  - for  $f_c'$  = 1.10-1.30
  - for  $F_y$  = 1.12-1.14 **(1.12)\***
  - for  $F_{pu}$  = 1.02-1.04
- **Coefficient of variation**
  - for  $f_c'$  = 11-17% **(15-18%)\***
  - for  $F_y$  = 2-3% **(10%)\***
  - for  $F_{pu}$  = 1.5% **(2.5%)\***

**\*NBS Report 577 (1980)**

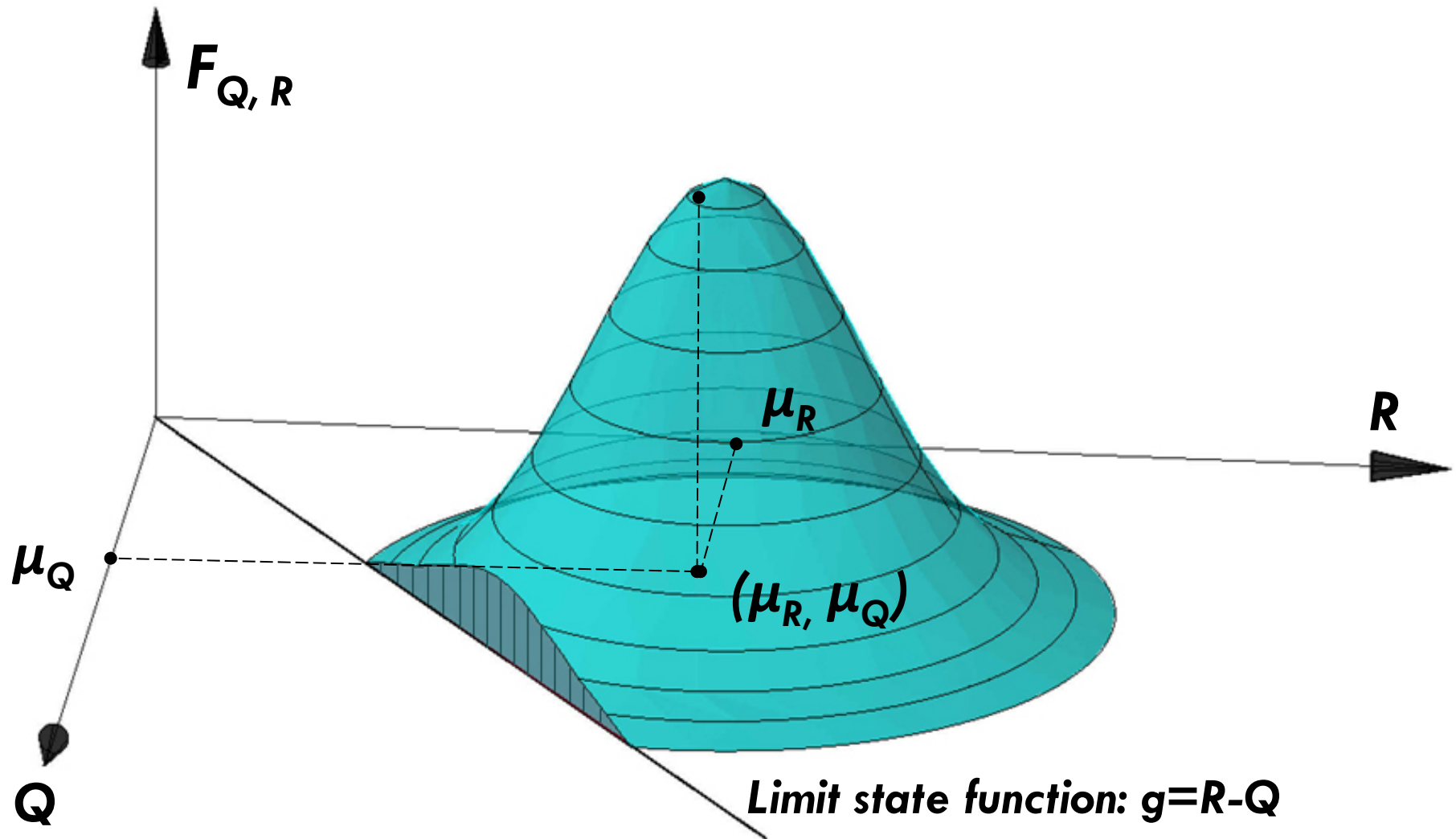
# Probability of Failure and Reliability Index $\beta$

$Q = \text{load}$  and  $R = \text{resistance}$

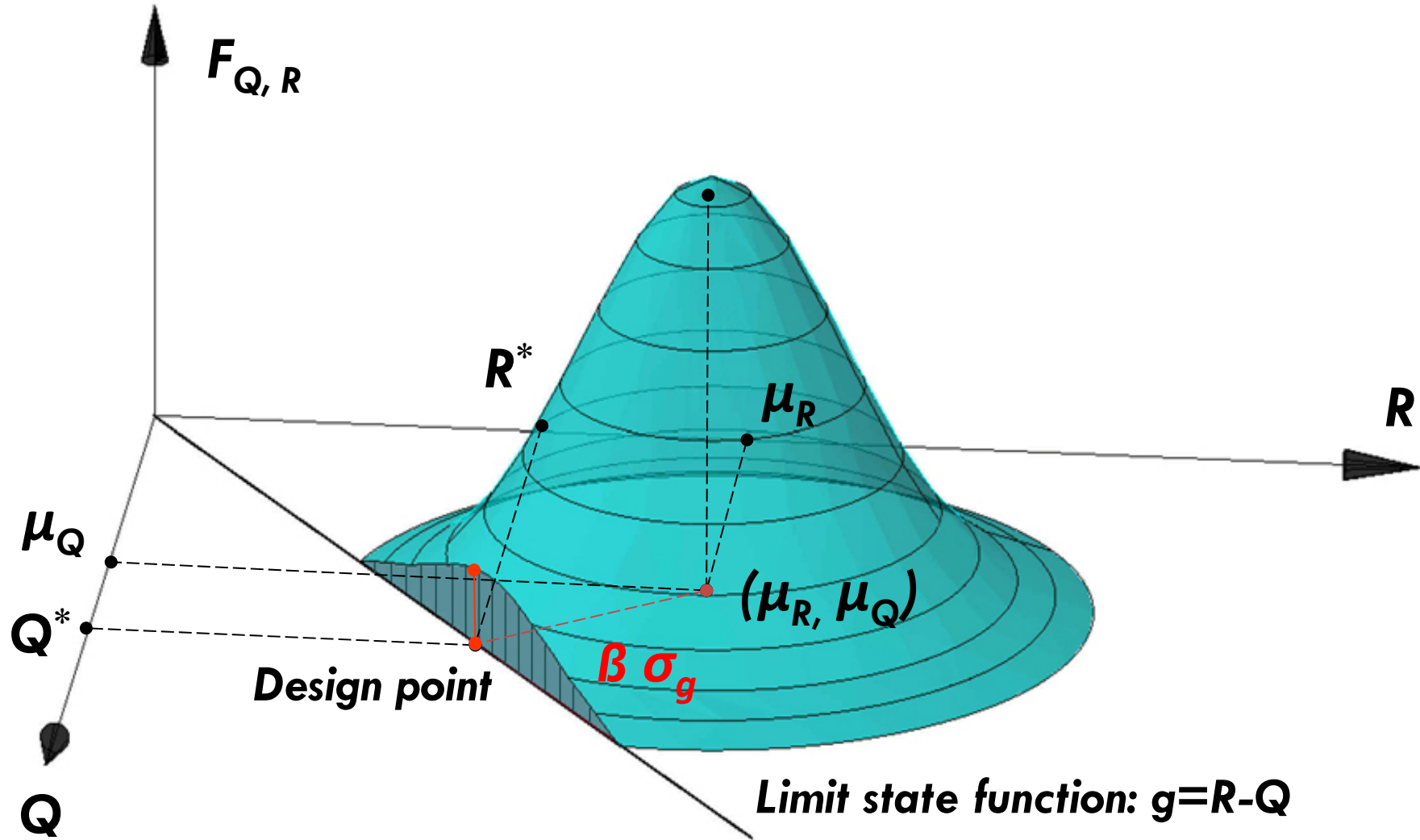


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# Fundamental case



# Fundamental case



# Reliability Index, $\beta$

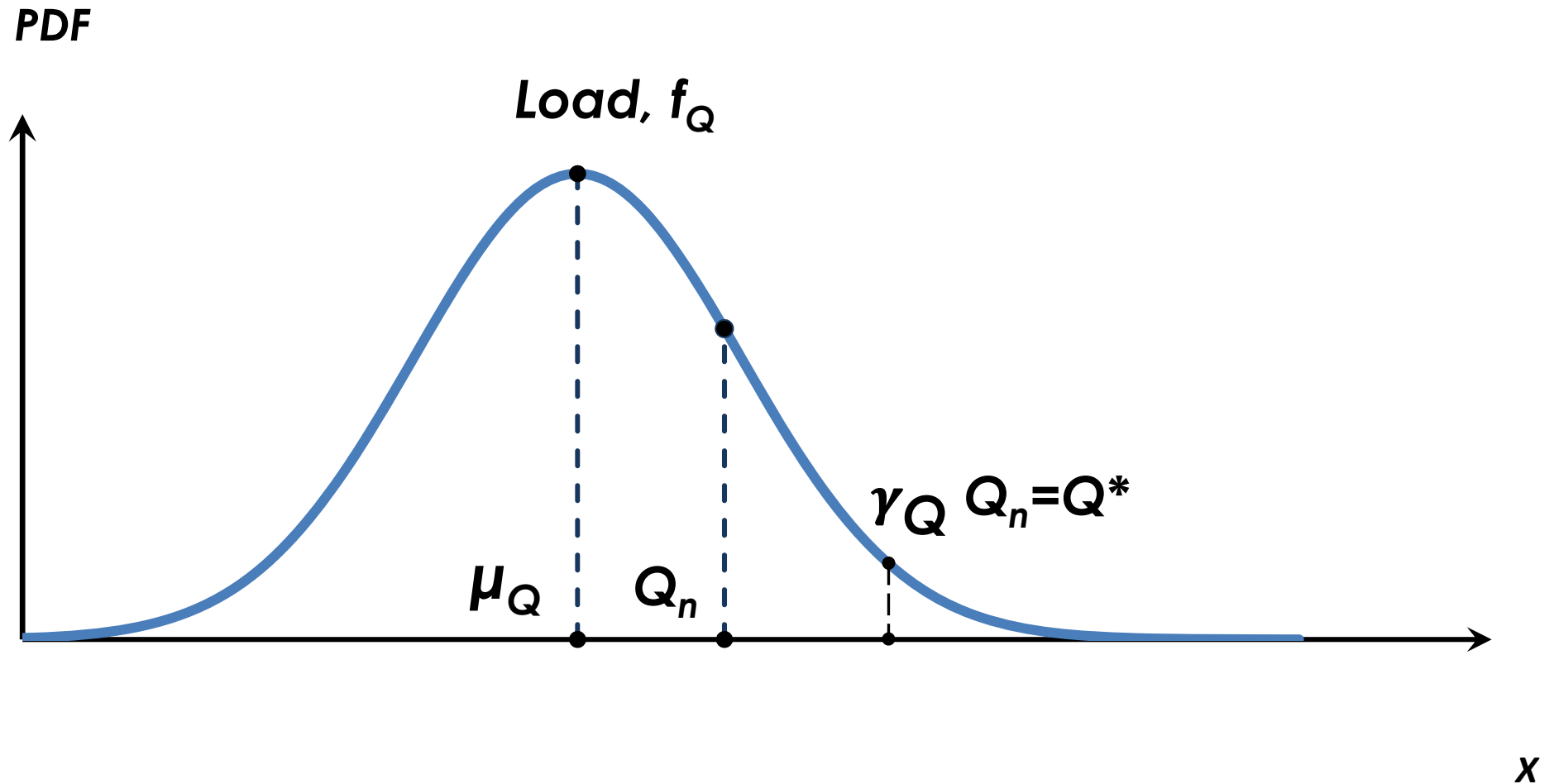
If the limit state function  $g = R - Q$ , then

$$\beta = \frac{\mu_R - \mu_Q}{\sqrt{\sigma_R^2 + \sigma_Q^2}}$$

$$\beta = -\Phi^{-1}(P_f) \quad \text{or} \quad P_f = \Phi(-\beta)$$

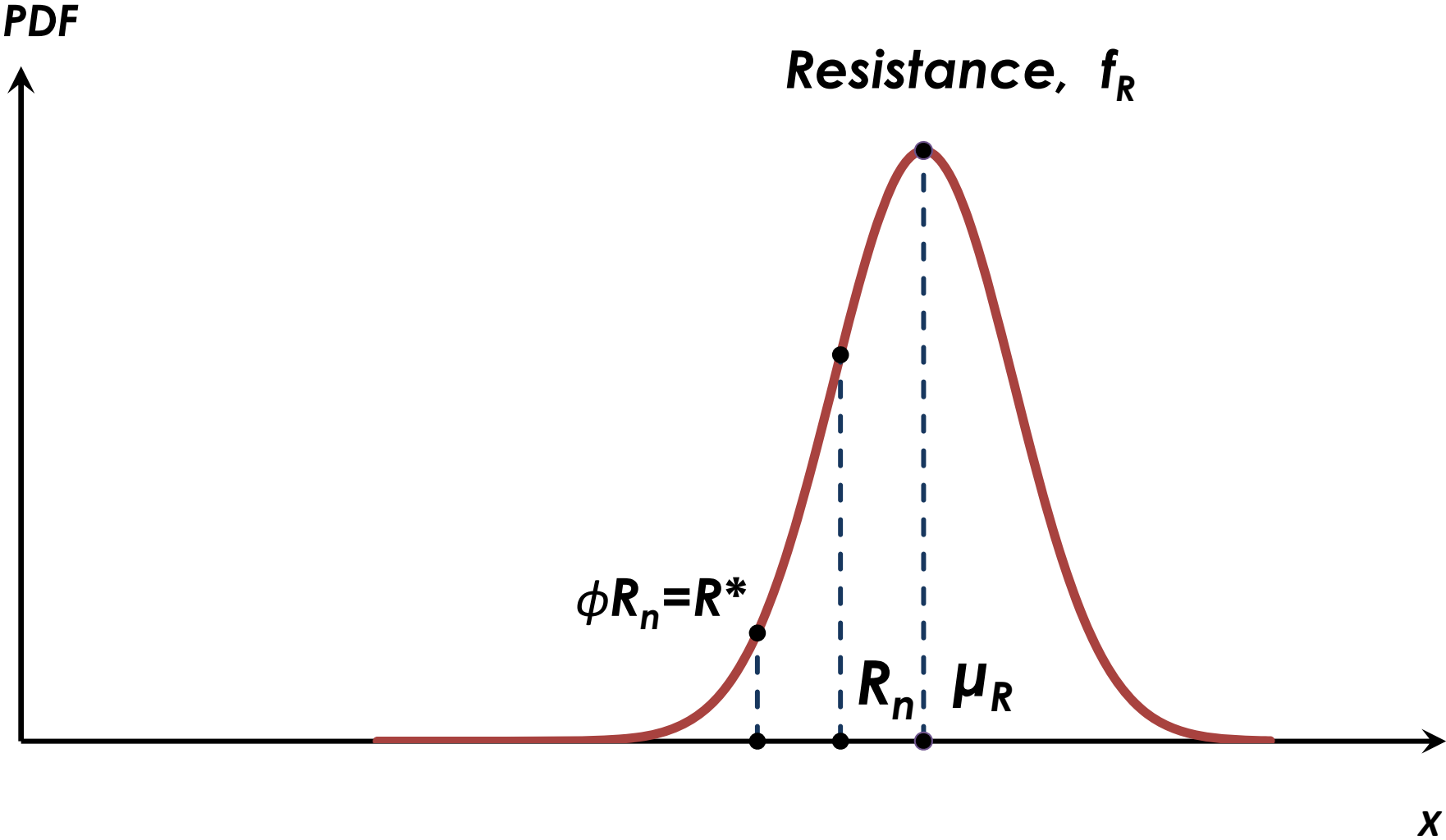
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# DESIGN POINT



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# DESIGN POINT



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# Design Point

The coordinate of the design point,  $R^*$

$$R^* = \mu_R - \beta \frac{\sigma_R^2}{\sqrt{\sigma_R^2 + \sigma_Q^2}}$$

$\mu_R$  = Mean value of resistance

$\sigma_R$  = Standard deviation of resistance

$\sigma_Q$  = Standard deviation of load

$\beta$  = Reliability Index

# Design Point

The coordinate of the design point,  $Q^*$

$$Q^* = \mu_Q + \beta \frac{\sigma_Q^2}{\sqrt{\sigma_R^2 + \sigma_Q^2}}$$

$\mu_Q$  = Mean value of load

$\sigma_R$  = Standard deviation of resistance

$\sigma_Q$  = Standard deviation of load

$\beta$  = Reliability Index

# Load Factor as Design Point

Calculate load factor,  $\gamma_Q$ :

$$\gamma_Q = \frac{\lambda_Q Q^*}{\mu_Q}$$

$$\gamma_Q = \frac{Q^*}{Q_n}$$

$Q_n$  = nominal value of  $Q$

$\lambda_Q$  = bias factor of  $Q$  (*ratio of mean to nominal*)

$Q^*$  = coordinate of the design point for  $Q$

$\mu_Q$  = mean value of  $Q$

# Resistance Factors as Design Point

Calculate resistance factor,  $\varphi$

$$\varphi = \frac{\lambda_R R^*}{\mu_R}$$

$$\varphi = \frac{R^*}{R_n}$$

$R_n$  = nominal value of  $R$

$\lambda_R$  = bias factor of  $R$  (*ratio of mean to nominal*)

$R^*$  = coordinate of the design point for  $R$

$\mu_R$  = mean value of  $R$

# Load Factors as Design Point

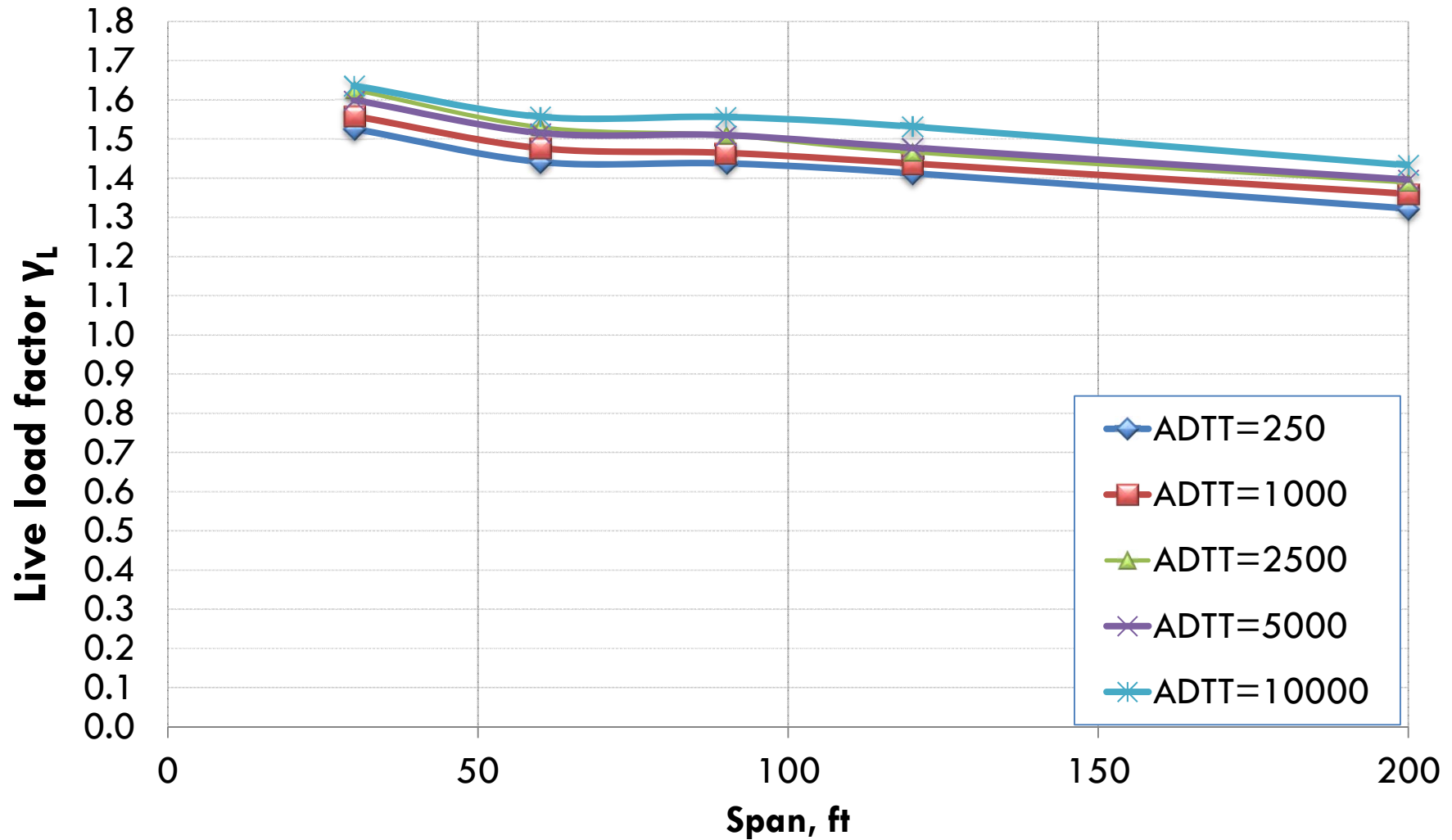
The dead load factors calculated are as follows:

for precast  $D_1$ ,  $\gamma_{D1} = 1.05-1.1$

for cast in place  $D_2$ ,  $\gamma_{D2} = 1.10-1.17$

for wearing surface  $D_w$   $\gamma_{Dw} = 1.03-1.1$

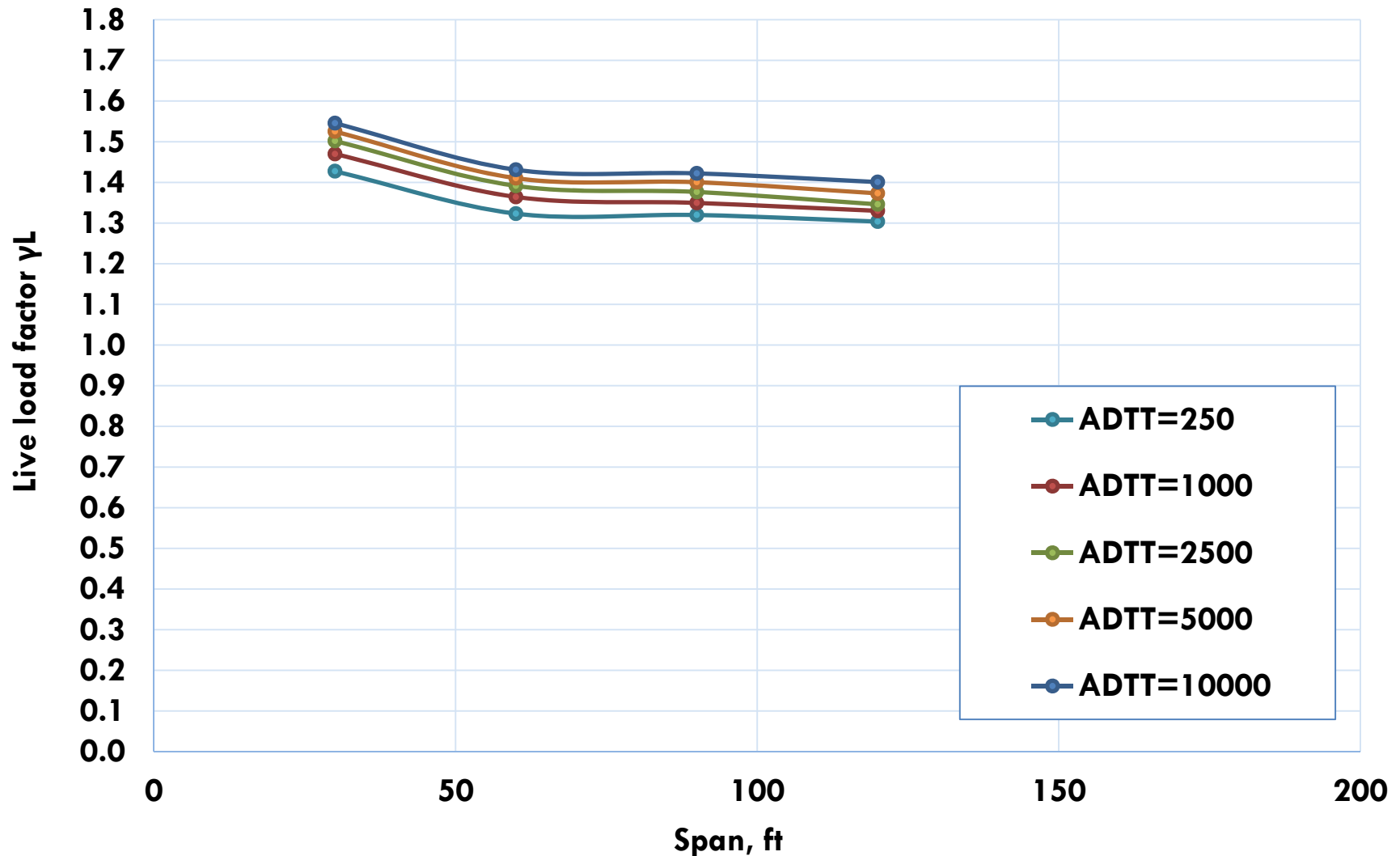
# Live Load Factor as Design Point



**Moment for Prestressed Concrete Girders**

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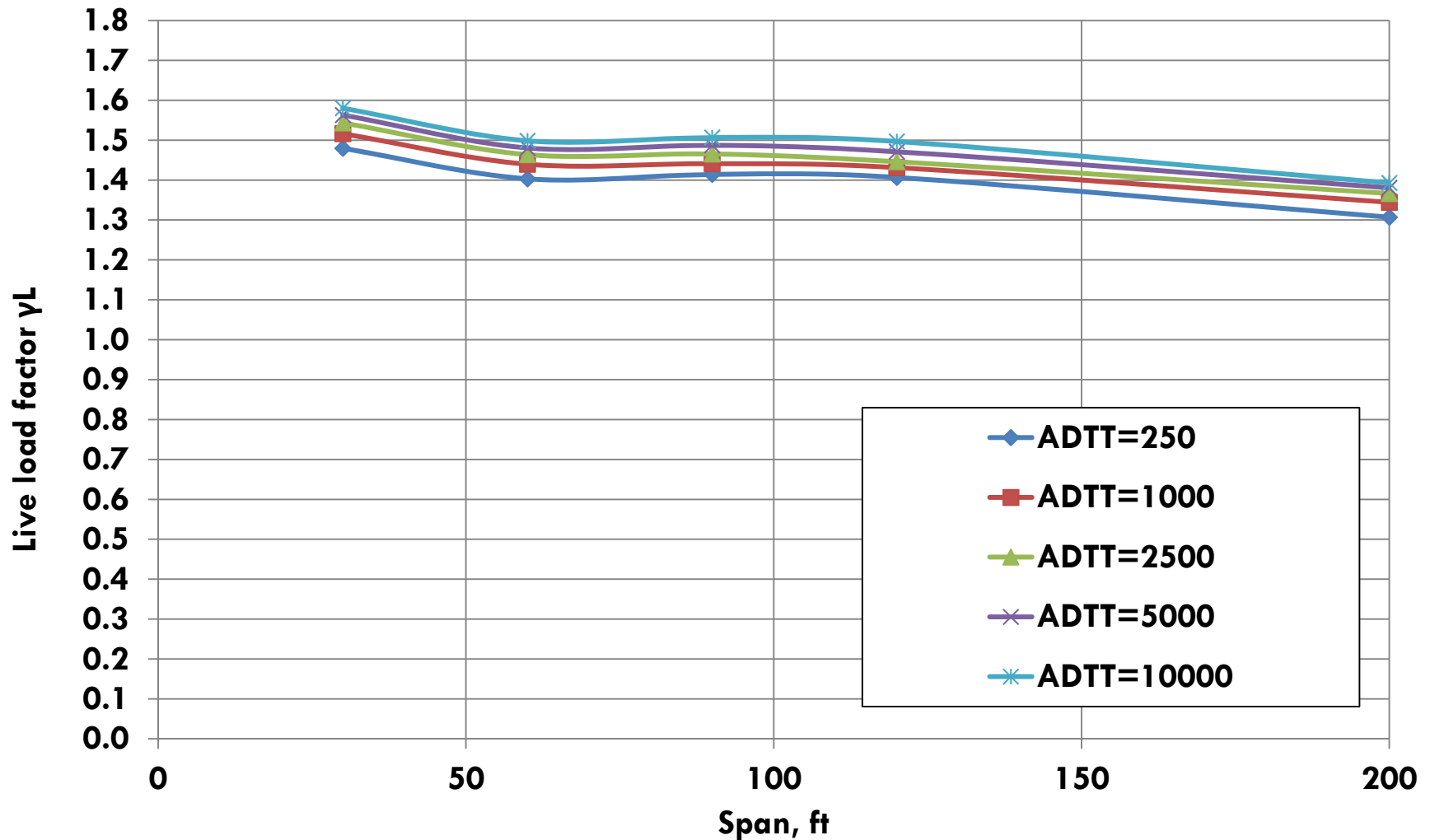
# Live Load Factor as Design Point



**Moment for Reinforced Concrete T-Beams**

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# Live Load Factor as Design Point

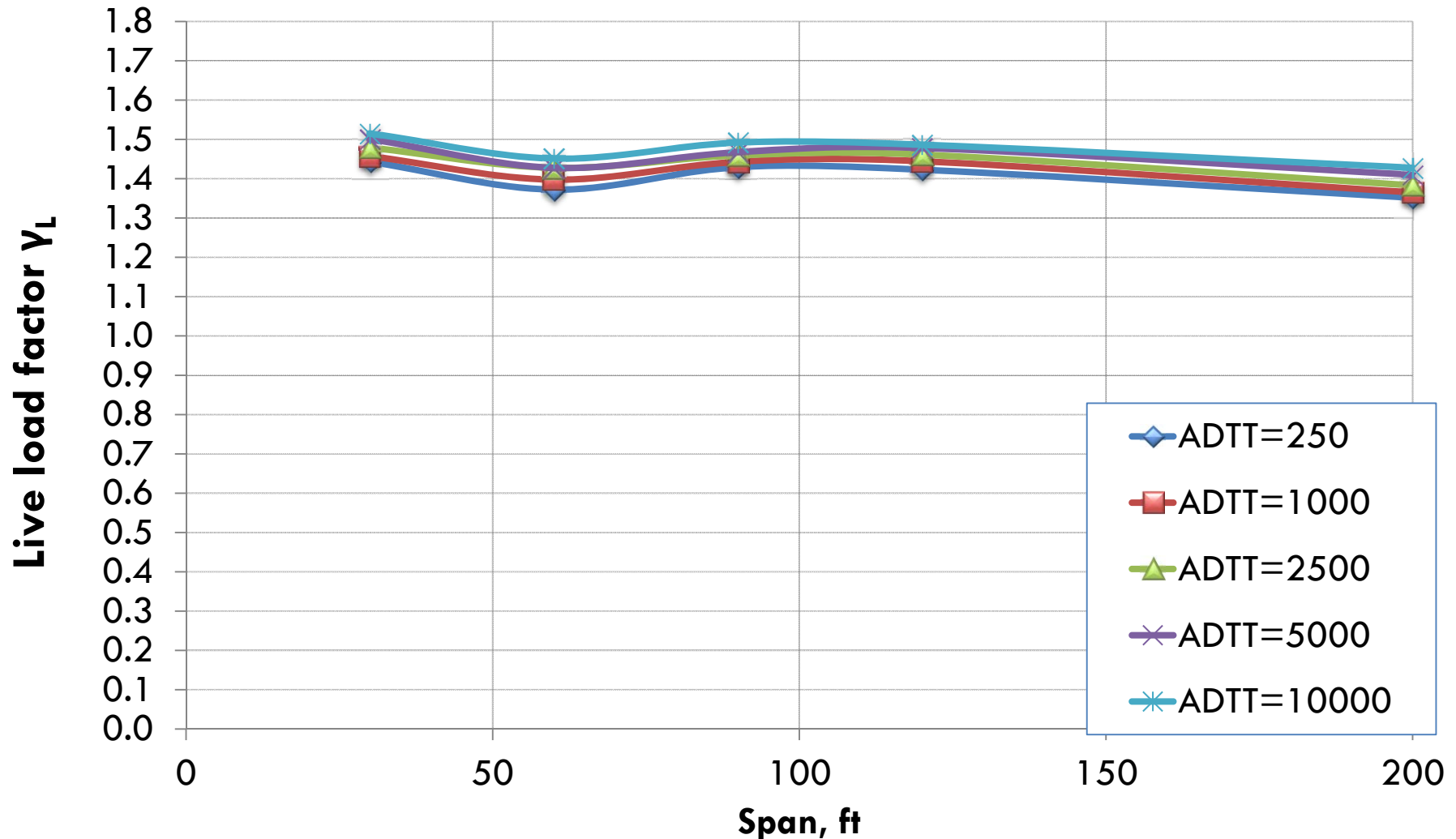


**Moment for Steel Girders**

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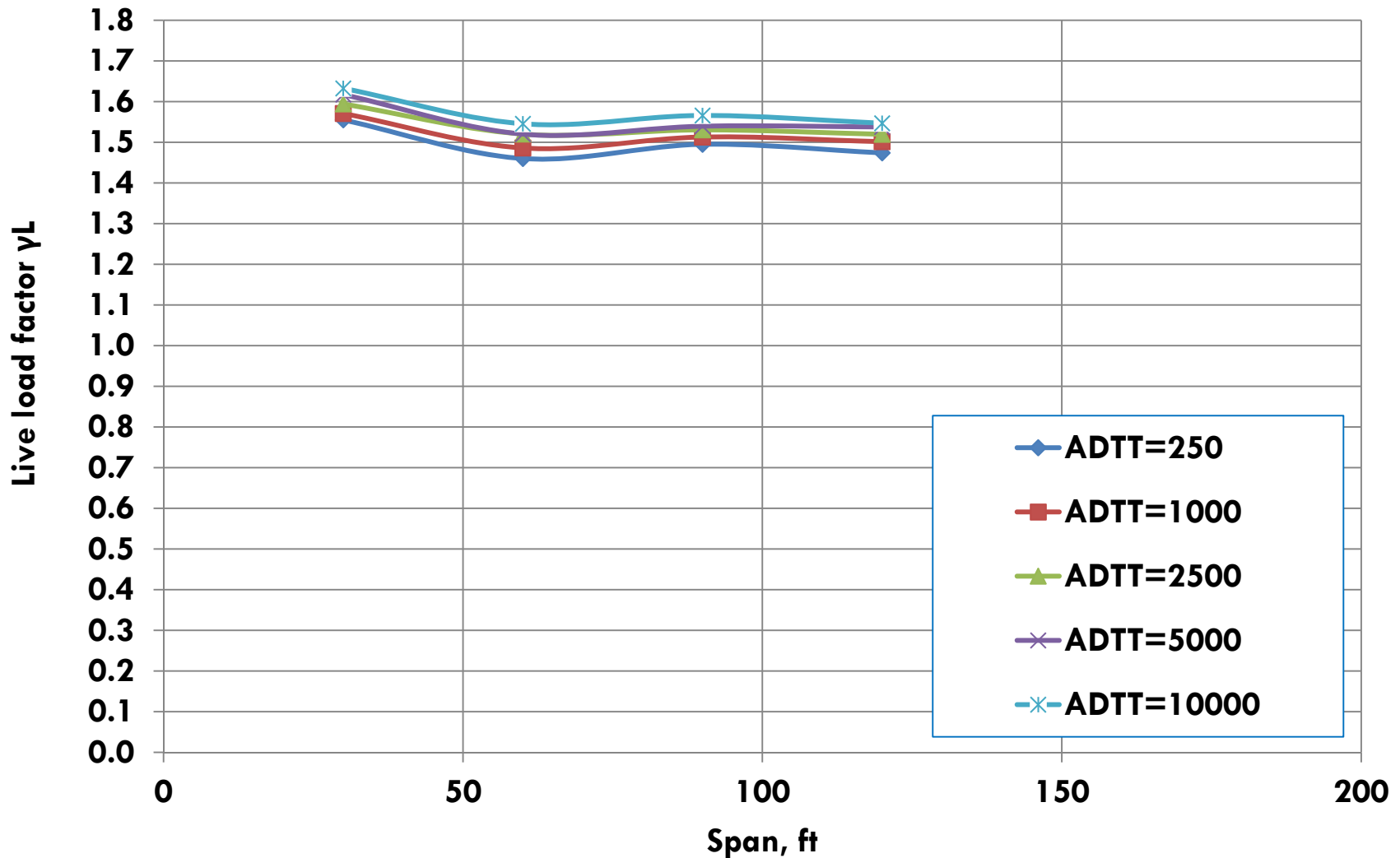
# Live Load Factor as Design Point



**Shear for Prestressed Concrete Girders**

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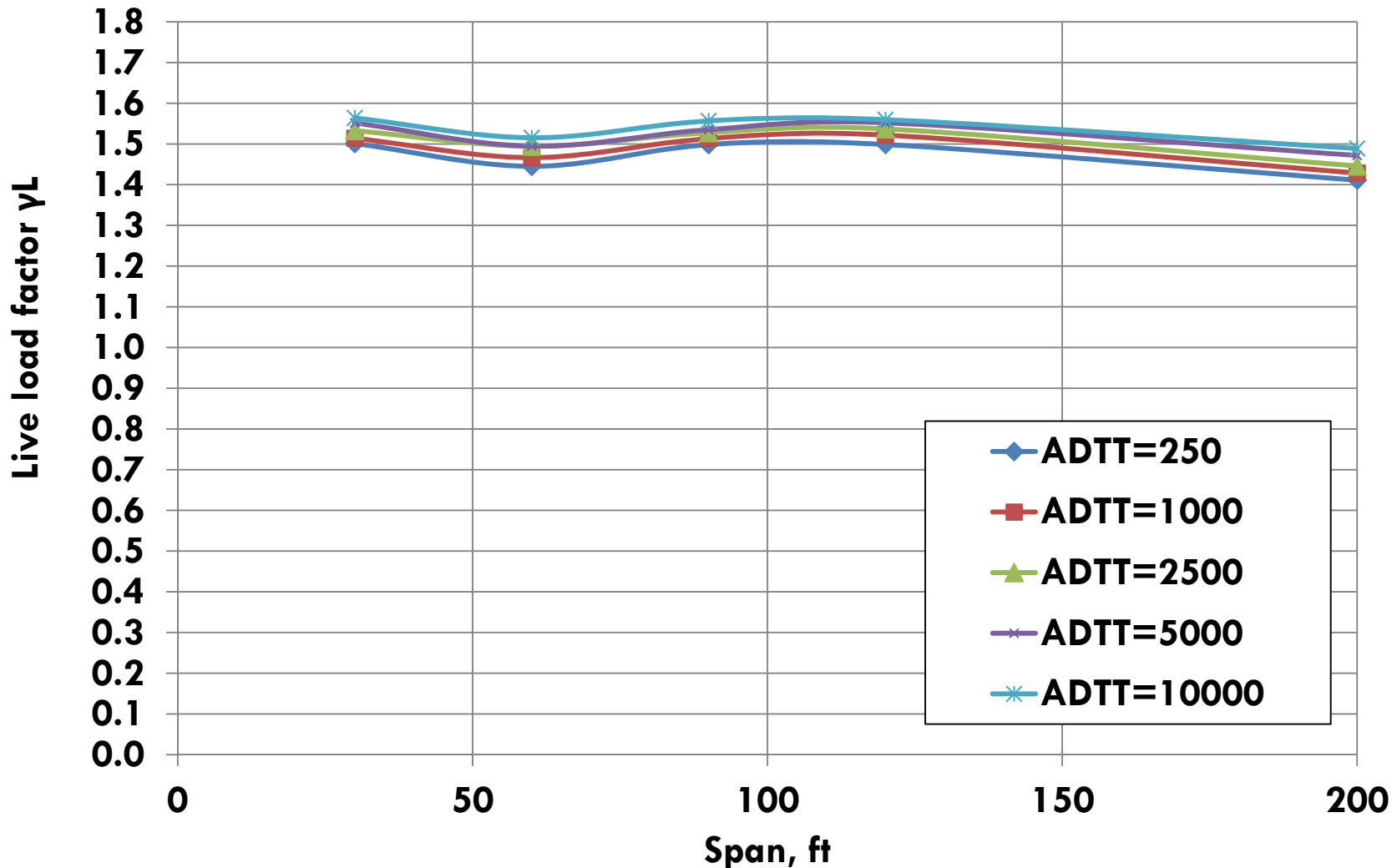
# Live Load Factor as Design Point



Shear for Reinforced Concrete T-Beams

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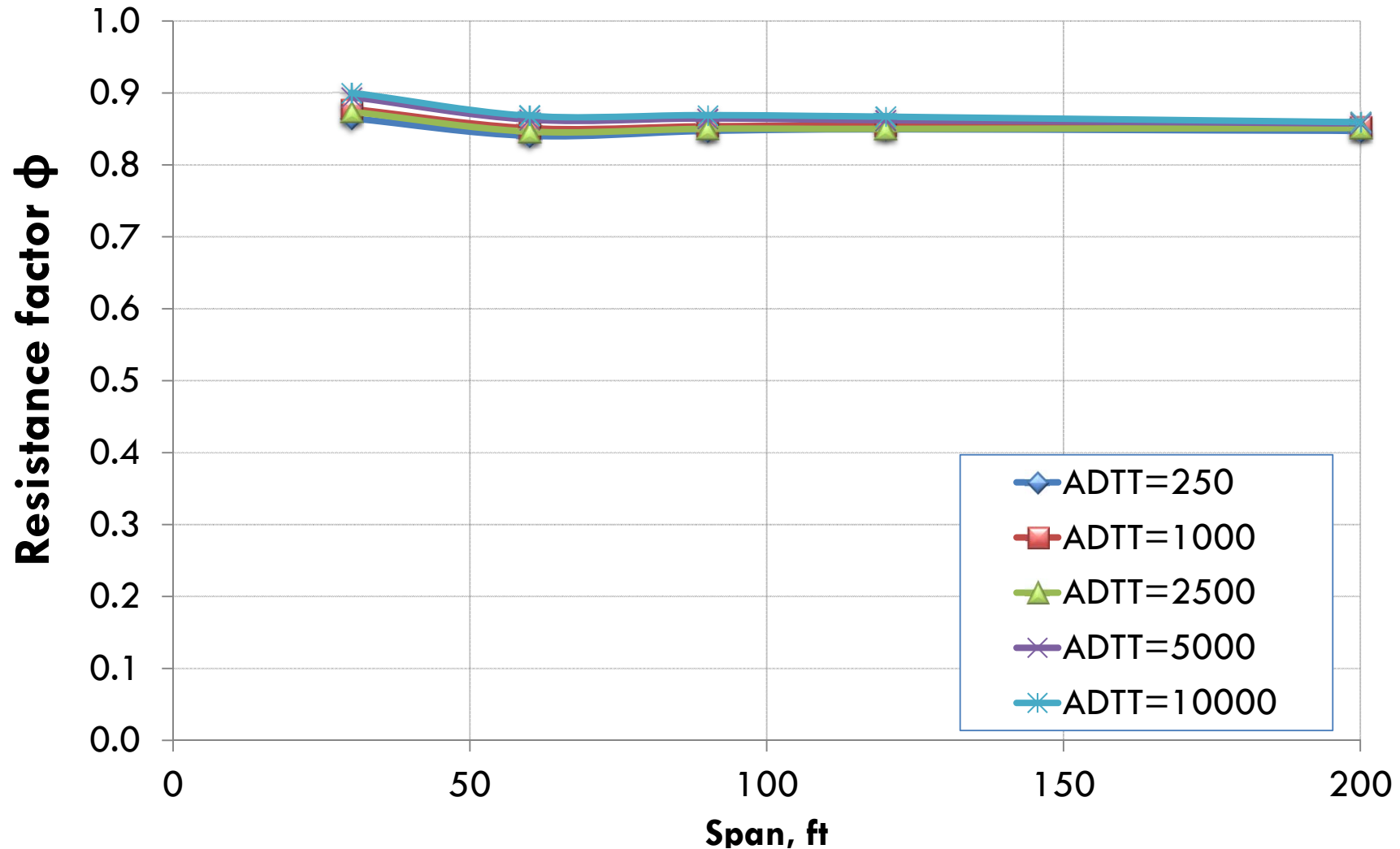
# Live Load Factor as Design Point



Shear for Steel Girders

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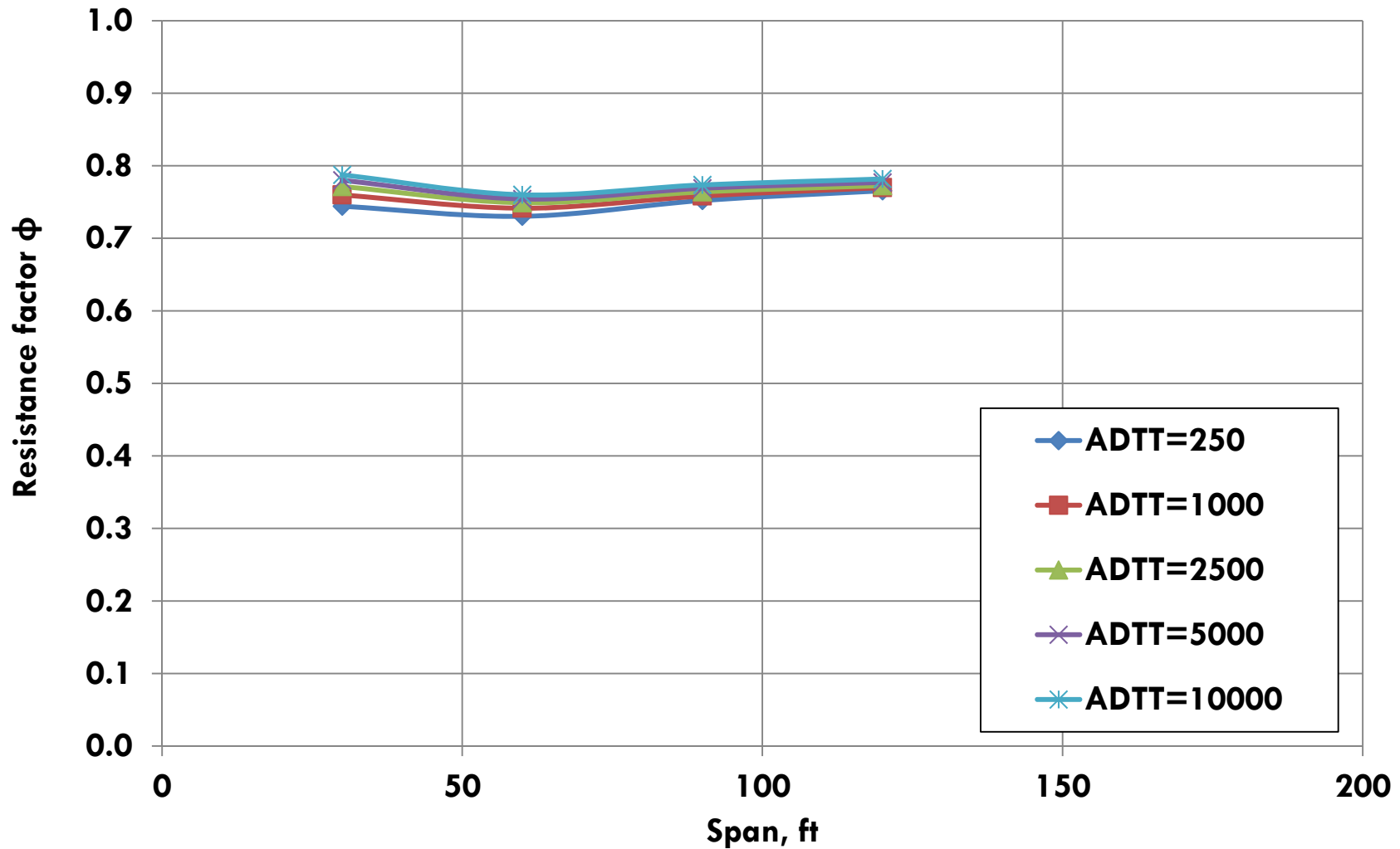
# Resistance Factor as Design Point



**Moment for Prestressed Concrete Girders**

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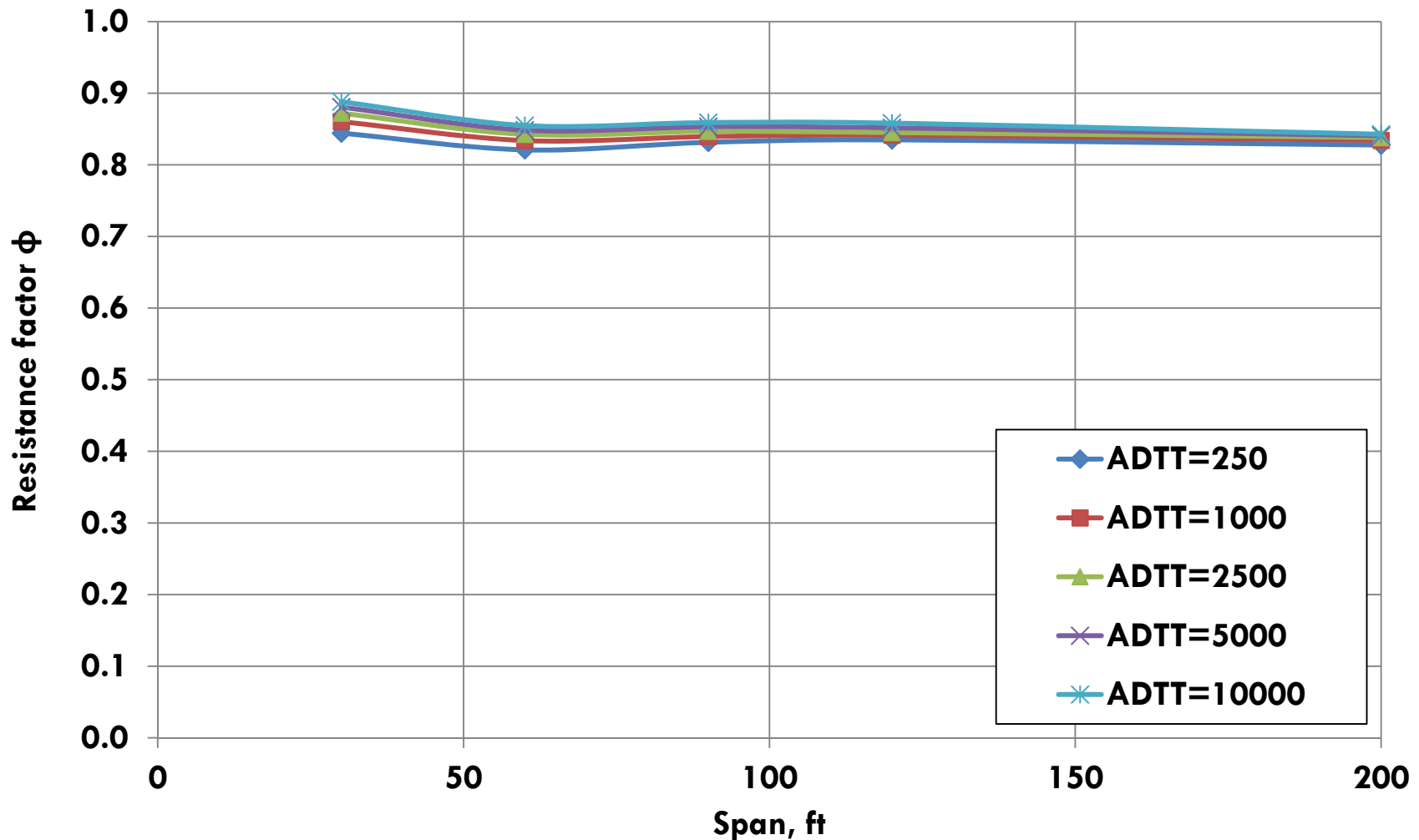
# Resistance Factor as Design Point



**Moment for Reinforced Concrete T-Beams**

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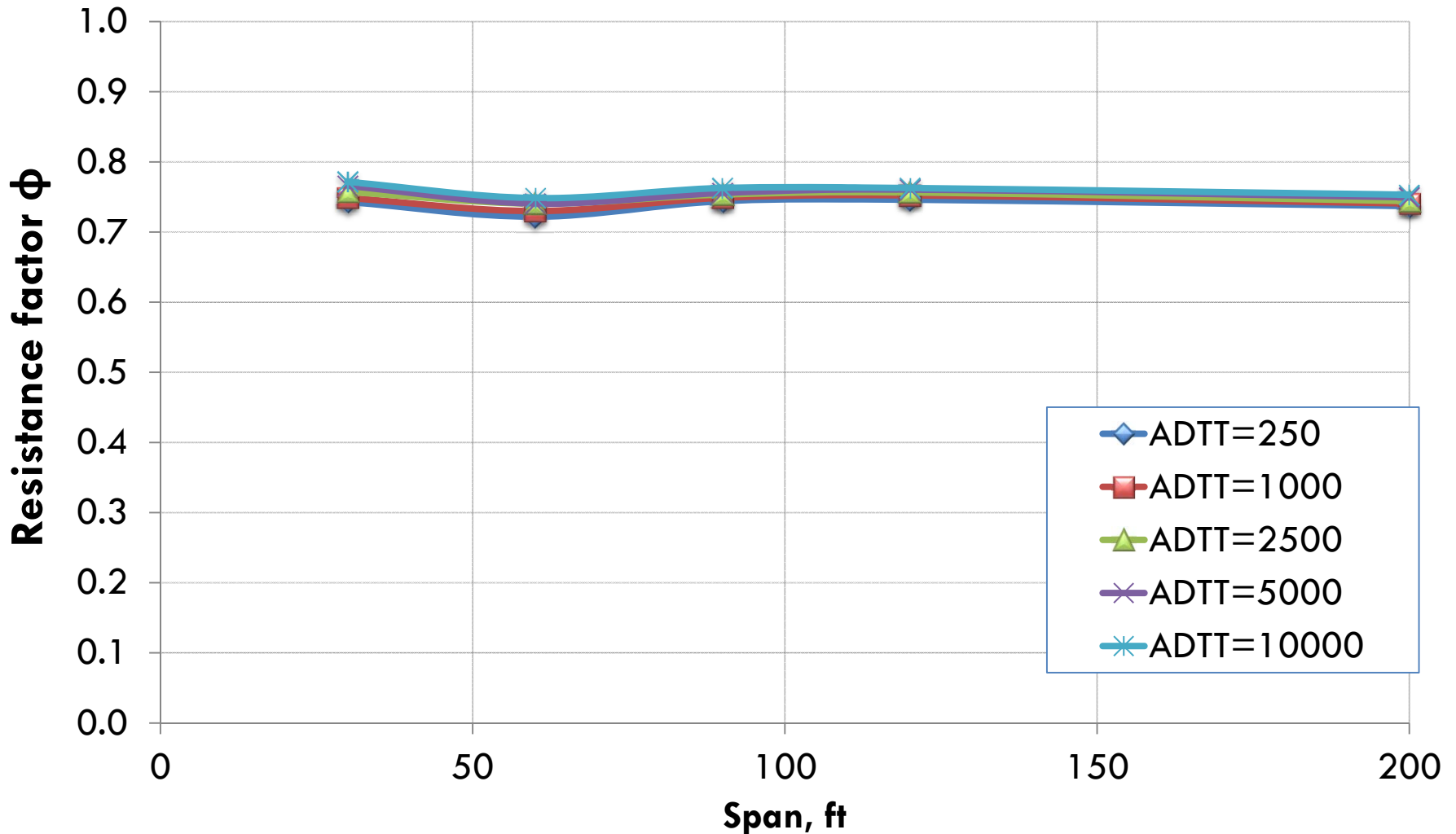
# Resistance Factor as Design Point



**Moment for Steel Girders**

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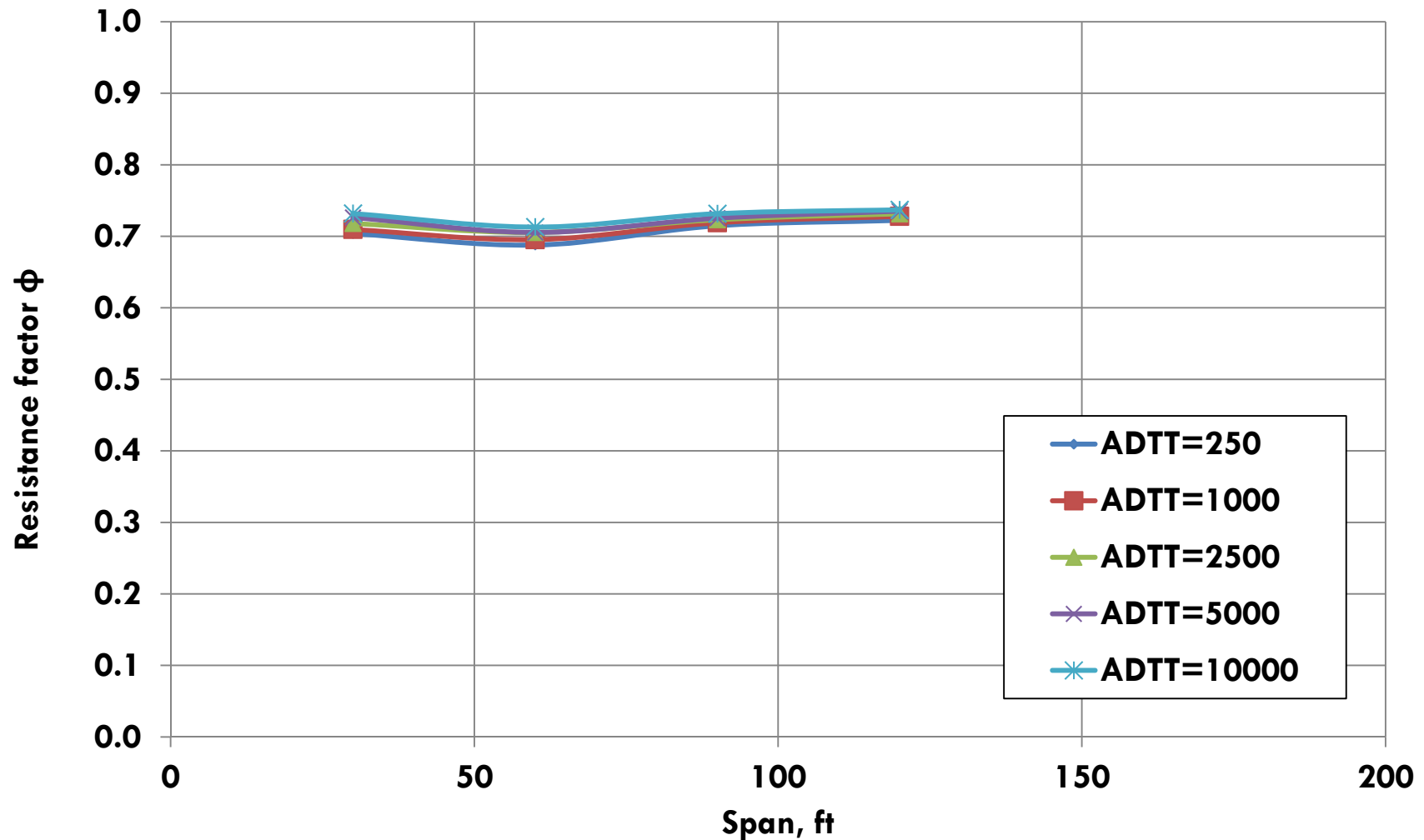
# Resistance Factor as Design Point



**Shear for Prestressed Concrete Girders**

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# Resistance Factor as Design Point

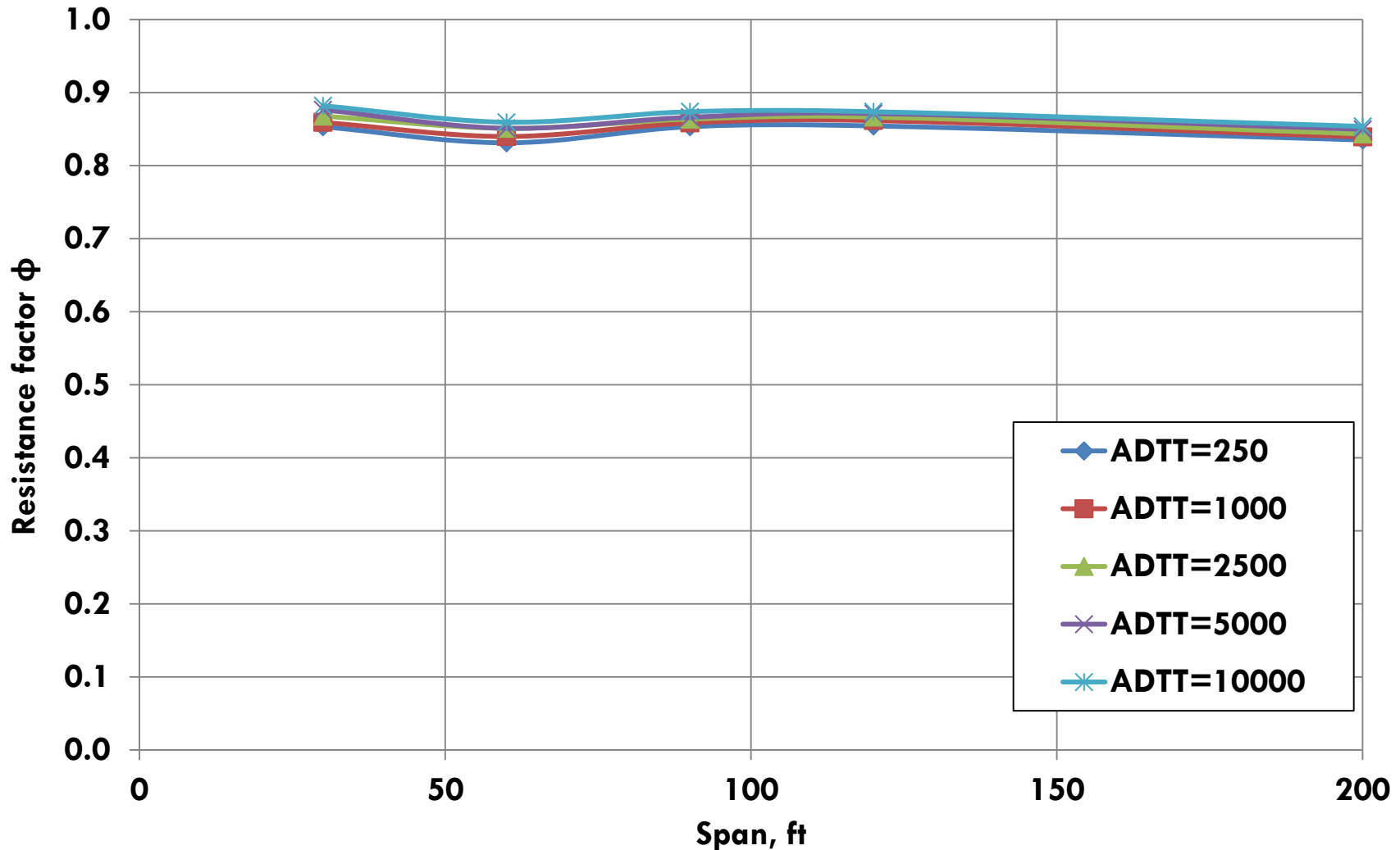


Shear for Reinforced Concrete T-Beams

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# Resistance Factor as Design Point



**Shear for Steel Girders**

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# Resistance Factor as Design Point

**Resistance factor for prestressed concrete:**

For moment:  $\phi = 0.85 - 0.9$

For shear:  $\phi = 0.75$

**Resistance factor for reinforced concrete:**

For moment  $\phi = 0.75 - 0.8$

For shear:  $\phi = 0.7$

**Resistance factor for steel:**

For moment  $\phi = 0.85 - 0.9$

For shear:  $\phi = 0.85$

# Considered Cases

## Current Design Formula

$$1.25 DC + 1.50 DW + 1.75 LL (1 + IM) \leq 1.00 R$$

If new updated/upgraded live load is used

**Live load factor = 1.90**

$$1.25 DC + 1.50 DW + 1.9 LL (1 + IM) \leq 1.00 R$$

# Considered Cases

## Current Design Formula

$$1.25 DC + 1.50 DW + 1.75 LL (1 + IM) \leq 1.00 R$$

If new updated/upgraded resistance statistics is used

$$\phi = 1.10$$

$$1.25 DC + 1.50 DW + 1.75 LL (1 + IM) \leq 1.10 R$$

# Considered Cases

## Current Design Formula

$$1.25 DC + 1.50 DW + 1.75 LL (1 + IM) \leq 1.00 R$$

If new updated/upgraded resistance and live load statistics are used

$$\phi = 1.05$$

# Design Point Factors

## Current Design Formula

$$1.25 \text{ DC} + 1.50 \text{ DW} + 1.75 \text{ LL} (1 + \text{IM}) \leq 1.00 \text{ R}$$

## Calculated Load Factors – new updated live load

$$1.15 \text{ DC} + 1.15 \text{ DW} + 1.55 \text{ LL} (1 + \text{IM}) \leq 0.85 \text{ R}$$

## Proposed Load Factors - new updated live load

$$1.20 \text{ DC} + 1.20 \text{ DW} + 1.60 \text{ LL} (1 + \text{IM}) \leq 0.90 \text{ R}$$

# Resistance Factors as Design Point

## Moment

Material	Resistance Factor in Current AASHTO LRFD $\phi$	Calculated Resistance Factor $\phi$	Recommended Resistance Factor $\phi$
Steel (Comp. and Non-comp.)	1.00	0.85	0.9
Prestressed concrete	1.00	0.85	0.9
Reinforced concrete	0.90	0.75	0.8

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# Resistance Factors as Design Point

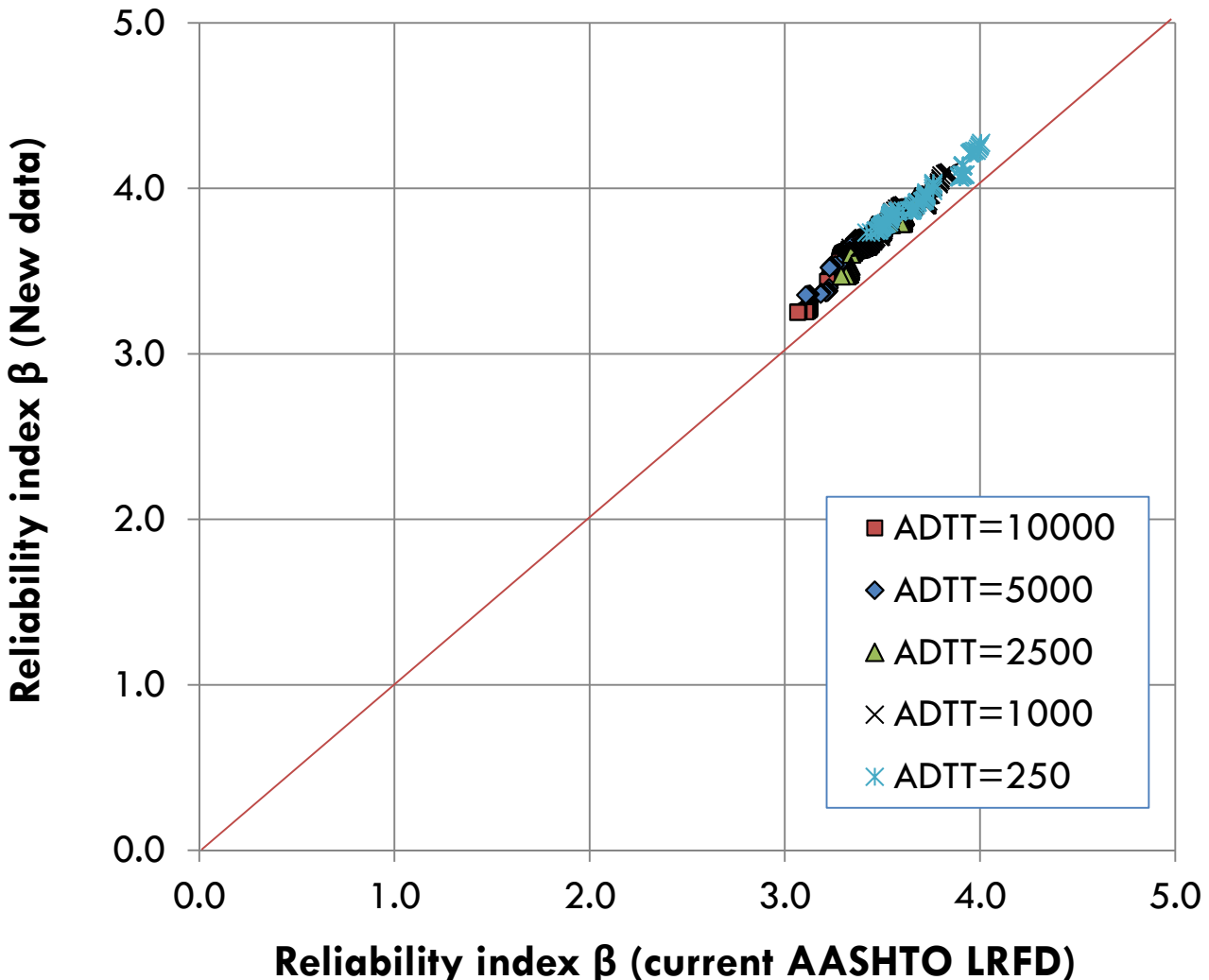
## Shear

Material	Resistance Factor in Current AASHTO LRFD $\phi$	Calculated Resistance Factor $\phi$	Recommended Resistance Factor $\phi$
Steel (Comp. and Non-comp.)	1.00	0.85	0.9
Prestressed concrete	0.9	0.75	0.8
Reinforced concrete	0.85	0.70	0.75



# Proposed Load Factors - new live load

$$1.20 DC + 1.20 DW + 1.60 LL (1 + IM) \leq 0.90 R$$



# Design Formula – to be confirmed by Re-Calibration, Steel and Prestressed Concrete

## Current Design Formula

$$1.25 \text{ DC} + 1.50 \text{ DW} + 1.75 \text{ LL} (1 + \text{IM}) \leq 1.00 \text{ R}$$

## Expected Factors - new updated/upgraded live load and resistance

$$1.20 \text{ DC} + 1.20 \text{ DW} + 1.60 \text{ LL} (1 + \text{IM}) \leq 0.95 \text{ R}$$